

Cos(ϕ) compensation

P	3000	Load Power [Watt]
U	230	Load rms Line-Neutral voltage
cos(ϕ)	0.75	Load cos(ϕ)
Rcable/meter	0.01	Cable resistance per meter[Ω per meter]
Lcable/meter	1.0E-5	Cable inductance per meter[H per meter]
Cable length	0	Cable length [meter]

Calculate

Calculate nominal power

Load parameters P and cos(ϕ) are defined for U without cable

$$\text{Apparent power per phase } S[\text{VA}] = P/\cos(\phi) = 4000[\text{VA}]$$

$$Q[\text{VAR}] = \sqrt{S^2 - P^2} = \sqrt{4000^2 - 3000^2} = 2646[\text{VAR}]$$

$$I_{\text{nom}}[\text{A}] = S/U = 4000/230 = 17.391[\text{A}]$$

Calculate load resistance

From P and I the load resistance is calculated:

$$R_{\text{load}}[\text{ohm}] = P/I^2 = 3000/(17.391^2) = 10[\text{ohm}]$$

Calculate load inductance

From reactive power, the load inductance is calculated

$$X_{\text{load}}[\text{ohm}] = Q/I^2 = 2646/(17.391^2) = 8.748[\text{ohm}]$$

$$L_{\text{load}}[\text{mH}] = X_{\text{load}}/(2\pi f) = 8.748/(2\pi \cdot 50) = 27.8[\text{mH}]$$

Calculate cable resistance and inductance

$$R_{\text{cable}}[\text{m}\Omega] = R_{\text{cable}}[\text{per meter}] * \text{length [per phase]} = 0.01 * 0 = 0[\text{m}\Omega]$$

$$L_{\text{cable}}[\text{mH}] = L_{\text{cable}}[\text{per meter}] * \text{length [per phase]} = 1.0E-5 * 0 = 0[\text{mH}]$$

$$X_{\text{cable}}[\Omega] = L_{\text{cable}} * 2\pi f = 1.0E-5 * 2\pi \cdot 50 = 0[\Omega]$$

$$Z_{\text{cable}}[\Omega] = \sqrt{(R_{\text{cable}})^2 + (X_{\text{cable}})^2} = \sqrt{0^2 + 0^2} = 0[\Omega]$$

Calculate total resistance and inductance seen from the source

$$R_{\text{tot}}[\Omega] = R_{\text{cable}} + R_{\text{load}} = 0 + 10 = 10[\Omega]$$

$$L_{\text{tot}}[\text{mH}] = L_{\text{cable}} + L_{\text{load}} = 0 + 0 = 27.844[\text{mH}]$$

$$X_{\text{tot}}[\Omega] = L_{\text{tot}} * 2 \pi f = 27.844 * 314.15927 = 8.748[\Omega]$$

$$Z_{\text{tot}}[\Omega] = \sqrt{(R_{\text{tot}}^2 + X_{\text{tot}}^2)} = \sqrt{(9.919^2 + 8.748^2)} = 13.225[\Omega]$$

Calculate new current

$$I_{\text{new}} = U/Z_{\text{tot}} = 230/13.225 = 17.39[\text{A}]$$

Calculate apparent power

$$S = U * I_{\text{new}} = 230 * 17.39 = 4000[\text{VA}]$$

Calculate Cable loss

$$R_{\text{cable}} * I_{\text{new}}^2 = 0 * 17.39^2 = 0[\text{Watt}]$$

Calculate power delivered to the load

$$R_{\text{load}} * I_{\text{new}}^2 = 10 * 17.39^2 = 3000[\text{Watt}]$$

Calculate Load voltage

$$U_{\text{load new}} = U - Z_{\text{cable}} * I_{\text{new}} = 230 - 0 * 17.39 = 230[\text{Volt}]$$

Calculate new $\cos(\phi)$

$$\cos(\phi) = (P_{\text{cable}} + P_{\text{load}})/S = (0 + 3000)/4000 = 0.75$$

Calculate Reactive power for calculating the compensation capacitor

$$Q[\text{VAR}] = \sqrt{S^2 - (P_{\text{cable}} + P_{\text{load}})^2} = \sqrt{4000^2 - 3000^2} = 2646[\text{VAR}]$$

Calculate compensation capacitor

$$X_C = U^2/Q = 230^2/2646 = 20[\Omega]$$

$$C = 1/(2\pi f X_C) = 1/(314.15927 * 20) = 159[\mu\text{F}]$$