

Cos(φ) compensation

P	3000	Load Power [Watt]
U	230	Load rms Line-Neutral voltage
cos(φ)	0.75	Load cos(φ)
Rcable/meter	0.01	Cable resistance per meter[Ω per meter]
Lcable/meter	1.0E-5	Cable inductance per meter[H per meter]
Cable length	100	Cable length [meter]
Calculate		

Calculate nominal power

Load parameters P and cos(φ) are defined for U without cable

Apparent power per phase $S[\text{VA}] = P/\cos(\phi)=4000[\text{VA}]$
 $Q[\text{VAR}] = \sqrt{S^2-P^2}=\sqrt{4000*4000-3000*3000}=2646[\text{VAR}]$
 $I_{\text{nom}}[\text{A}] = S/U=4000/230=17.391[\text{A}]$

Calculate load resistance

From P and I the load resistance is calculated:
 $R_{\text{load}}[\text{ohm}]=P/I^2=3000/(17.391*17.391)=10[\text{ohm}]$

Calculate load inductance

From reactive power, the load inductance is calculated
 $X_{\text{load}}=Q/I^2=2646/(17.391*17.391)=8.748[\text{ohm}]$
 $L_{\text{load}}[\text{mH}]=X_{\text{load}}/(2 \pi f)=9/314.15927=27.8[\text{mH}]$

Calculate cable resistance and inductance

$R_{\text{cable}}[\text{m}\Omega]=R_{\text{cable}}[\text{per meter}] * \text{length} [\text{per phase}]=10*100=1000[\text{m}\Omega]$
 $L_{\text{cable}}[\text{mH}]=L_{\text{cable}}[\text{per meter}] * \text{length} [\text{per phase}]=0.01*100=1[\text{mH}]$
 $X_{\text{cable}}[\Omega]=L_{\text{cable}} * 2 \pi f=1*314.15927=0.314[\Omega]$
 $Z_{\text{cable}}[\Omega]=\sqrt{R_{\text{cable}}^2+X_{\text{cable}}^2}=\sqrt{1*1+0.314*0}=1.048[\Omega]$

Calculate total resistance and inductance seen from the source

$R_{\text{tot}}[\Omega]=R_{\text{cable}}+R_{\text{load}}=1+10=10.919[\Omega]$

$$L_{\text{tot}}[\text{mH}] = L_{\text{cable}} + L_{\text{load}} = 1 + 0 = 28.844[\text{mH}]$$

$$X_{\text{tot}}[\Omega] = L_{\text{tot}} * 2 \pi f = 28.844 * 314.15927 = 9.062[\Omega]$$

$$Z_{\text{tot}}[\Omega] = \sqrt{R_{\text{tot}}^2 + X_{\text{tot}}^2} = \sqrt{10.919^2 + 9.062^2} = 14.189[\Omega]$$

Calculate new current

$$I_{\text{new}} = U / Z_{\text{tot}} = 230 / 14.189 = 16.21[\text{A}]$$

Calculate apparent power

$$S = U * I_{\text{new}} = 230 * 16.21 = 3728[\text{VA}]$$

Calculate Cable loss

$$R_{\text{cable}} * I_{\text{new}}^2 = 1 * 16.21 * 16.21 = 263[\text{Watt}]$$

Calculate power delivered to the load

$$R_{\text{load}} * I_{\text{new}}^2 = 10 * 16.21 * 16.21 = 2606[\text{Watt}]$$

Calculate Load voltage

$$U_{\text{load new}} = U - Z_{\text{cable}} * I_{\text{new}} = 230 - 1 * 16.21 = 213[\text{Volt}]$$

Calculate new cos(φ)

$$\cos(\phi) = (P_{\text{cable}} + P_{\text{load}}) / S = (263 + 2606) / 3728 = 0.77$$

Calculate Reactive power for calculating the compensation capacitor

$$Q[\text{VAR}] = \sqrt{S^2 - (P_{\text{cable}} + P_{\text{load}})^2} = \sqrt{3728^2 - 2868.89^2} = 2381[\text{VAR}]$$

Calculate compensation capacitor

$$X_c = U^2 / Q = 230^2 / 2381 = 22[\Omega]$$

$$C = 1 / (2\pi * f * X_c) = 1 / (314.15927 * 22) = 143[\mu\text{F}]$$